SEMESTER - I			
CORE - II MATHEMATICAL PHYSICS - I			
Code: 17PPHC12	Hrs/Week: 6	Hrs/Semester: 90	Credits:5

#### **Course Outcomes**

CO No.	Upon completion of this course, students will be able to	PSOs addressed	CL
CO 1	Calculate the area of irregular shape by Green's theorem	PSO2	E
CO 2	Design feedback control systems with finite dimensional vector spaces	PSO2	С
CO 3	Apply special functions for Wireless communication and alternating current transmission	PSO5	А
CO 4	Understand the geometry interpretation of complex numbers	PSO6	U
CO 5	Resolve the incompleteness of the statistical interpretations relating to the summing of an infinite number of probabilities to yield a meaningful solutions	PSO2	С
CO 6	Be familiar with the main mathematical methods used in physics.	PSO 7	R

#### **Unit I: Vector Calculus**

Review of Vector Algebra – Gradient of a scalar field - Divergence of a vector function - Curl of a vector function – Gauss Divergence theorem – Stokes's theorem – Green's theorem (Proof only). Linear vector space: Liner independence of vector and dimension – Basis of expansion theorem – Inner product and unitary spaces –Orthonormal sets – Schmidt's orthogonalisation method.

#### Unit II: Linear Algebra

Matrices: Review - Special types - Transpose - Conjugate – Conjugate Transpose - Symmetric and AntiSymmetric - Hermitian and Skew-Hermitian - Determinant - Singular and Non-Singular - Adjoint – Inverse - Orthogonal - Unitary - Trace - Rank - Cramer's rule - Eigen values, Eigenvectors: Characteristic equation of a Matrix - Cayley-Hamilton theorem.

#### **Unit III: Special Functions I and Partial Differential Equations**

Legendre Function: Legendre's Equation - Generating Function – Rodrigue's Formula – Orthogonality - Recurrence Formulae - Bessel Function: Bessel's Function of the First kind – Generating Function – Recurrence Formulae.

Introduction - Laplace equation (Cartesian - 3D only) – Heat flow equation (3D only) - Equation motion for the vibrating string (D'Alembert's solution only).

#### **Unit IV: Complex Analysis**

Complex variables– Limits and continuity – Differentiability –Analytic function- Cauchy-Riemann equations(necessary and sufficient condition, polar form)– Cauchy theorem – Cauchy

integral formula – Taylor's theorem – Laurent theorem - Singular points – Residues – Method of finding residues- Residue theorem – Evaluation of definite integrals(unit circle type & evaluation  $\int_{-\infty}^{+\infty} \frac{f_1(x)}{f_2(x)} dx$  only).

# Unit V: Group Theory

Group, subgroup, classes – invariant, subgroups, factor groups –homomorphism and isomorphism – grouprepresentation – reducible and irreducible representation – Schur's lemmas, great orthogonality theorem – character table.

Continuous Groups: Lie groups and lie algebra – SO (3) group – SU (2) and SU (3) unitary groups. **Books for study:** 

- 1. Satya Prakash, Mathamatical Physics, Sultan Chand & Sons, New Delhi.
- 2. H.K.Dass ,Mathematical Physics, S.Chand & Company LTD, Fourth Revised Edition 2004
- 3. Mathematical Physics, P.K. Chattopadhyay, New Age International Publishers, Reprint (2001)

Unit	Book No.	Chapters / Sections
Ι	1	1.1,1.2,1.4,1.5,1.7,1.9,1.12,1.16
II	1	2.2, 2.5-2.11, 2.14, 2.19, 2.23, 2.27, 2.31-2.32
III	1	6.7-6.11,6.17,6.21,6.22,8.2,8.11,8.13
IV	2	7.3-7.10,7.31-7.33, 7.39-7.47
V	3	8.1-8.7, 8.11-8.13

#### **Books for reference:**

- 1. Erwin Kreyszig, Advanced Engineering Mathematics, John Wiley and sons (Asia), 8<sup>th</sup> Edition (2005).
- 2. B. D Gupta, Mathematical Physics, Vikas Publishing house PVT LTD, Fourth Edition 2010

SEMESTER - II			
CORE IV MATHEMATICAL PHYSICS II			
Code: 17PPHC21	Hrs/Week: 6	Hrs/Semester: 90	Credits: 4

#### **Course Outcomes**

CO No.	Upon completion of this course, students will be able to	PSOs addressed	CL
CO 1	Analyse the experimental data with the aid of Fourier transform	PSO5	An
CO 2	Understand the basic of tensor calculus and to describe motion and deformation of body	PSO2	U
CO 3	Recall the basic notations of generating functions and special functions	PSO1	R
CO 4	Apply computational techniques to solve a wide range of numerical problems arising in physics	PSO3	А
CO 5	Explain the concepts of Green's functions and solve boundary value problems	PSO1	Е
CO 6	Solve Linear Differential Equations of First and Second order	PSO2	A

#### **Unit I: Probability and Integral Transforms**

Probability: Probability – definitions - Binomial distribution, Poisson distribution – Gaussian distribution.

Integral Transforms: Fourier Series- Fourier integral – Fourier transform - Linearity – first and second shifting theorems – Laplace transform – transforms of derivative and integral – inverse Laplace transform – partial fractions.

#### **Unit II: Tensors**

Notations and conventions – tensors of second rank – equality and null tensor – addition and substraction – outer product of tensors – inner product of tensors – symmetric and antisymmetric tensor – Kronecker delta – quotient law – metric tensor – Cartesian tensor – isotropic tensor – stress, strain and Hooke's law.

#### **Unit III: Special Functions II**

Hermite functions: Hermite Differential Equation – Hermite Polynomials – Recurrence Formulae – Rodrigue's Formula – Orthogonality.Laguerre function: Differential equation – Laguerre polynomial – Generating Function – Rodrigue's Formula – Recurrence Relation – Orthogonal Property.

#### **Unit IV: Numerical methods**

Solution of Algebraic and Transcendental equations: Newton – Raphson's method - Solution of Linear Algebraic Equations: Gauss elimination, Interpolation: Lagrange's interpolation– Inverse interpolation – Finite differences– Newton's forward and backward interpolation - Numerical

Integration :Trapezoidal rule - Simpson's 1/3<sup>rd</sup> and 3/8<sup>th</sup> rule - Initial Value Problems:Solving first order differential equations using Runge-Kutta methods.

## Unit V: Greens Function and Linear differential equations of first & Second Order

Green's function for one dimensional problems and properties – Green's function in higher dimensions. Application: Poisson's equation.

Linear differential equations –Equations of first order and higher degree-Linear differential equations of second order with constant coefficients – Method for finding the complementary function – Rules to find particular integral.

### **Books for study:**

- 1. Satya Prakash, Mathematical Physics, Fourth revised Edition 2004, Sultan Chand & Sons.
- 2. Matrices and tensors in Physics, A.W. Joshi, New Age International Publishers, Revised Third Edition (1995), Reprint 2010.
- 3. Numerical Methods A. Singaravelu, Meenakshi Agency, Chennai
- 4. P.K. Chattopadhyay, Mathematical Physics, New Age International Publishers, Reprint (2001) and [Unit-V Chapter 6].
- 5. H.K.Dass ,Mathematical Physics, S.Chand & Company LTD, Fourth Revised Edition 2004

Unit	Book No.	Chapters / Sections
Ι	1	11.2, 11.20, 11.21, 11.22, 7.1, 7.3, 7.5, 7.6, 7.10, 9.2, 9.3, 9.9, 9.11,
		9.12, 9.15, 9.20
II	2	15.2, 15.5, 16.1-16.4, 16.6, 16.7, 17,18.1, 19.3-19.5
III	1	6.29, 6.31 - 6.33, 6.35 - 6.38
IV	3	1.1, 1.16, 1.53, 2.1, 2.13, 2.59, 2.61, 2.75, 3.27, 3.31, 4.54
V	4	6.2, 6.5, 6.6,
	5	3.14-3.18

## **Books for reference:**

- 1. Erwin Kreyszig, Advanced Engineering Mathematics, John Wiley and sons (Asia), 8<sup>th</sup> Edition (2005).
- 2. B D Gupta, Mathematical Physics, Vikas Publishing house PVT LTD, Fourth Edition 2010

SEMESTER - I					
CORE - II Mathematical Physics – I					
Code: 19PPHC12	Code : 19PPHC12Hrs/Week: 6Hrs/Semester: 90Credits:4				

### Vision

To make the students competent and capable problem solvers using techniques that requires mathematical skills and an understanding of limiting cases.

### Mission

To analyze and visualize the solution in terms of special functions and how to use in practice the Bessel functions, Legendre polynomial.

### **Course Outcome:**

CO No.	Upon completion of this course, students will be able to	PSO	CL
		addressed	
CO 1	evaluate the area of irregular shape by Green's theorem.	2	Ev
CO 2	recall the basic and the special types of matrices.	1	Re
CO 3	understand the concepts of feedback control systems with finite	7	Un
	dimensional vector spaces.		
CO 4	apply special functions for Wireless communication and	2	Ар
	alternating current transmission.		_
CO 5	understand the geometrical interpretation of complex numbers.	1	Un
CO 6	explain the characteristic equation of a matrix using Cayley	3	Ev
	Hamilton Theorem.		
CO 7	recall the incompleteness of the statistical interpretations	2	Re
	relating to the summing of an infinite number of probabilities to		
	yield a meaningful solution.		
CO 8	apply group theory to various disciplines of Physics.	3	Ap

SEMESTER - I			
CORE - II	Mathematical P	hysics – I	
Code : 19PPHC12	Hrs/Week: 6	Hrs/Semester: 90	Credits:4

### **Unit I: Vector Calculus**

Review of Vector Algebra – Gradient of a scalar field - Divergence of a vector function - Curl of a vector function – Gauss Divergence theorem – Stokes's theorem – Green's theorem (Proof only).

### Unit II: Linear Algebra

Matrices: Review - Special types - Transpose - Conjugate – Conjugate Transpose - Symmetric and AntiSymmetric - Hermitian and Skew-Hermitian - Determinant - Singular and Non-Singular - Adjoint – Inverse - Orthogonal - Unitary - Trace - Rank - Cramer's rule - Eigen values, Eigenvectors: Characteristic equation of a Matrix - Cayley-Hamilton theorem.

### **Unit III: Special Functions I and Partial Differential Equations**

Legendre Function: Legendre's Equation - Generating Function – Rodrigue's Formula – Orthogonality - Recurrence Formulae - Bessel Function: Bessel's Function of the First kind – Generating Function – Recurrence Formulae.

Introduction - Laplace equation (Cartesian - 3D only) – Heat flow equation (3D only) - Equation motion for the vibrating string (D'Alembert's solution only).

## **Unit IV: Complex Analysis**

Complex variables– Limits and continuity – Differentiability –Analytic function- Cauchy-Riemann equations(necessary and sufficient condition, polar form)– Cauchy theorem – Cauchy integral formula – Taylor's theorem – Laurent theorem - Singular points – Residues – Method of finding residues- Residue theorem – Evaluation of definite integrals(unit circle type & evaluation  $\int_{-\infty}^{+\infty} \frac{f_1(x)}{f_2(x)} dx$  only).

## **Unit V: Group Theory**

Group, subgroup, classes – invariant, subgroups, factor groups –homomorphism and isomorphism – group representation - reducible and irreducible representation – Schur's lemmas, great orthogonality theorem – character table.

#### **Text Books:**

- 1. Satya Prakash, Mathamatical Physics, Sultan Chand & Sons, New Delhi.
- 2. H.K.Dass, Mathematical Physics, S.Chand & Company LTD, Fourth Revised Edition 2004
- 3. P.K. Chattopadhyay, Mathematical Physics, New Age International Publishers, Reprint (2001)

Unit	Book No.	Chapters / Sections
Ι	1	1.1,1.2,1.4,1.5,1.7,1.9,1.12
II	1	2.2, 2.5-2.11, 2.14, 2.19, 2.23, 2.27, 2.31-2.32
III	1	6.7-6.11,6.17,6.21,6.22,8.2,8.11,8.13
IV	2	7.3-7.10,7.31-7.33, 7.39-7.47
V	3	8.1-8.7

# **Books for Reference:**

- 1. Erwin Kreyszig, Advanced Engineering Mathematics, John Wiley and sons (Asia), 8<sup>th</sup> Edition (2005).
- 2. B. D Gupta, Mathematical Physics, Vikas Publishing house PVT LTD, Fourth Edition 2010

SEMESTER - II			
Core VIII Mathematical Physics II			
Code: 19PPHC22	Hrs/Week: 5	Hrs/Semester: 75	Credits: 4

### Vision:

To introduce students to methods of mathematical physics and to develop required mathematical skills to solve problems in quantum mechanics, electrodynamics and other fields of theoretical physics.

### Mission:

To enhance the knowledge in probability, integral transforms special functions, tensors and numerical methods.

## **Course Outcome**

CO No.	Upon completion of this course, students will be able to	PSO addressed	CL
CO - 1	analyse the experimental data with the aid of Fourier transform	4	An
CO - 2	understand the basic of tensor calculus and to describe motion	1	Un
	and deformation of body		
CO - 3	recall the basic notations of generating functions and special	1	Re
	functions		
CO - 4	apply computational techniques to solve a wide range of	2	Ap
	numerical problems arising in physics		
CO - 5	explain the concepts of Laplace Integral	1	Un
CO - 6	solve mathematical problems arising in physics by a variety of	2	Cr
	mathematical techniques.		
CO - 7	employ the knowledge of critical thinking and problem solving	5	Ap
CO - 8	employ correct method to solve a particular problem	2	Ap

SEMESTER - II			
Core VIII	II Mathematical Physics II		
Code: 19PPHC22	Hrs/Week: 5	Hrs/Semester: 75	Credits: 4

### Unit I: Probability and Fourier's Integral Transforms

Probability: Probability- definitions - Binomial distribution, Poisson distribution, normal distribution.

Fourier Integral Transforms: Fourier transform- properties of FT-FT of a derivative-Finite FT

### **Unit II: Tensors**

Notations and conventions-contravariant vector-covariant vector- tensors of second rank – equality and null tensor- addition and substraction – outer product of tensors- inner product of tensors- symmetric and antisymmetric tensor- metric tensor- Cartesian tensor- isotropic tensor- stress, strain and Hooke's law-Moment of inertia tensor.

### **Unit III: Special Functions II**

Hermite functions: Hermite Differential Equation– Hermite Polynomials– Recurrence Formulae– Rodrigue's Formula-Laguerre function: Differential equation– Laguerre polynomial – Generating Function– Rodrigue's Formula– Recurrence Relation.

#### **Unit IV: Numerical methods**

Solution of non - linear equation: Newton – Raphson's method - Solution of Linear Algebraic Equations: Gauss elimination, Interpolation: Lagrange's interpolation– Inverse interpolation – Finite differences– Newton's forward and backward interpolation - Numerical Integration: Trapezoidal rule - Simpson's 1/3<sup>rd</sup> and 3/8<sup>th</sup> rule - Runge-Kutta method(Fourth order).

## **Unit V: Laplace's Integral Transforms**

Laplace transform-properties of Laplace transform-Laplace transforms of derivative of a function- Laplace transform of integral - inverse Laplace transform-properties of inverse Laplace transform- Evaluation of ILT by convolution theorem- Method of partial fractions for evaluation of ILT

Unit	Book No.	Pages/sections	
Ι	1	11.2,11.20,11.21,9.2,9.3,9.4,9.7	
II	2	15.2,15.3,15.4,15.5,16.1,16.2,16.3,16.4,16.6,18.1,19.3,19.4,19.5,19.7	
III	1	6.29,6.30,6.31,6.32,6.34,6.35,6.36,6.37	
IV	3	1.1, 1.16, 1.53, 2.1, 2.13, 2.59, 2.61, 2.75, 3.27, 3.31	
V	1	9.9,9.10,9.11,9.15,9.17,9.18,9.19,9.20	

## **Text Books:**

- 1. Satya Prakash, Mathematical Physics, Fourth revised Edition 2004, Sultan Chand & Sons.
- 2. Matrices and tensors in Physics, A.W. Joshi, New Age International Publishers, Revised Third Edition (1995), Reprint 2010.
- 3. Numerical Methods A. Singaravelu, Meenakshi Agency, Chennai
- 4. P.K. Chattopadhyay, Mathematical Physics, New Age International Publishers, Reprint (2001) and
- 5. H.K.Dass ,Mathematical Physics, S.Chand & Company LTD, Fourth Revised Edition 2004.